

Calculating transformer turns

Say we have a transformer with an iron core of 10x10 cm cross-section (0.01m²)

max flux density of iron is around 1T so the maximum flux allowed is:

$$\phi_{\max} = 0.01 * 1 = 0.01\text{Wb}$$

the transformer operates at 230Vrms @50Hz meaning:

$$V_{\text{peak}} = 230 * \sqrt{2} = 325\text{V} \quad \text{and} \quad \omega = 2\pi f = 2\pi * 50 = 314$$

the flux waveform can be represented as:

$$\phi(t) = 0.01\sin(314t)$$

“rate of change” is the derivative in maths, which is:

$$\phi'(t) \text{ (or } d\phi/dt) = 3.14\cos(314t)$$

we want to know the rate of change at $t = 0.01\text{s}$ (max negative slope)

$$\phi'(0.01) = 3.14\cos(314 * 0.01) = -3.14$$

Plug this into Faraday's law with our peak voltage:

$$V = -N * d\phi/dt = 325 = -N * -314$$

we can then calculate that $N = 103$

This is the long way round. Doing all the maths it turns out you can combine everything into one neat equation, known by some as the transformer EMF equation:

$$V_{\text{rms}} = 4.44 * f * \phi_{\max} * N$$

filling in our numbers:

$$4.44 * 50 * 0.01 * 103 = 230\text{Vrms} \quad (\text{which is indeed the correct voltage})$$